

MACCCR Third Annual Fuels Summit

Chemistry and Transport Properties for Jet Fuel Combustion

K. Chae, J. Lai, A. Violi

Department of Mechanical Engineering

University of Michigan

Funding from AFOSR under supervision of Dr. J. Tishkoff

Tuesday, October 12, 2010



Role of diffusion

Ignition characteristics of $n\text{-C}_7\text{H}_{16}$ ^[1]

- 10% perturbation of diffusivity
→ 50K change of ignition temperature
- Sensitivity of ignition to diffusion \approx sensitivity to kinetics

Extinction of CH_4 /air flame^[2]

- Analysis with average and multiple diffusion models
→ 20 ~ 40% discrepancies in extinction strain rate

[1] M. G. Andac et. al., *31th Int. Sym. Combust.*, 2007, pp. 1165

[2] H. Wang et. al., *Combust. and flame*, 2005, Vol 142, pp. 374

Approaches to determine diffusion properties

Experiment

Very little



Gas Chromatographic (GC)

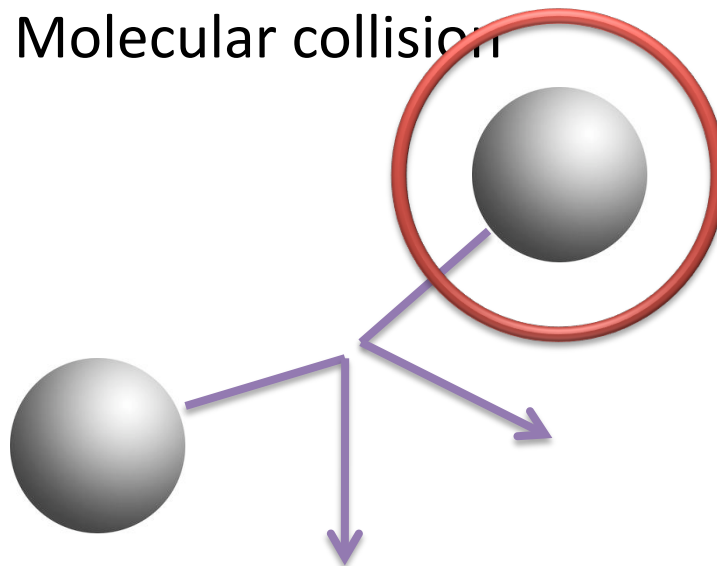
Theory



Gas Kinetic Theory (GKT)



Molecular collision



Spherical molecules



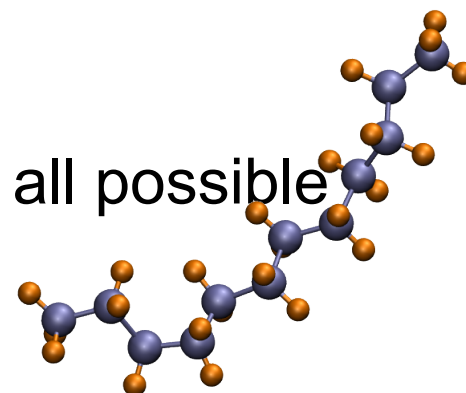
Simple analytical equation

$$D_{12} = \frac{3}{8} \frac{\sqrt{(k_B T)^3 / (2\pi m_{12})}}{n\sigma_{12}^2 \langle \Omega^{(1,1)*} \rangle}$$

Polyatomic Molecules

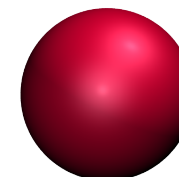
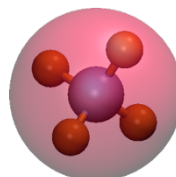
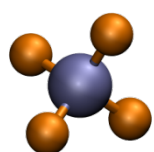
Dynamics of Molecular Collisions

- Have internal degrees of freedom. Collision can involve change in rotation and vibration energies.
- Interact through non-spherical intermolecular pair potential energies.
- Internal degrees of freedom for transporting energy – in GKT/C-E only binary elastic collisions are considered without internal degrees of freedom
- Collision integrals must be averaged over all possible relative orientations occurring in collision.

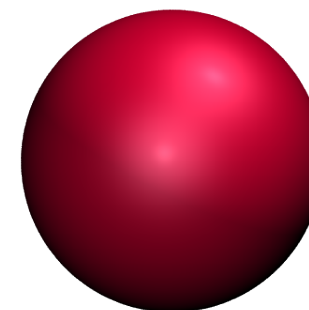
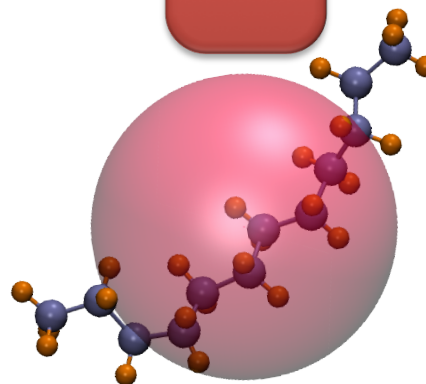
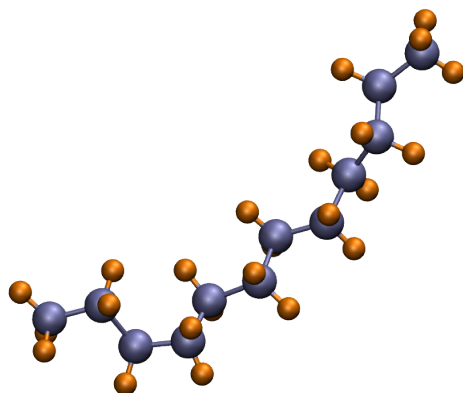


Validity of GKT

Simple...

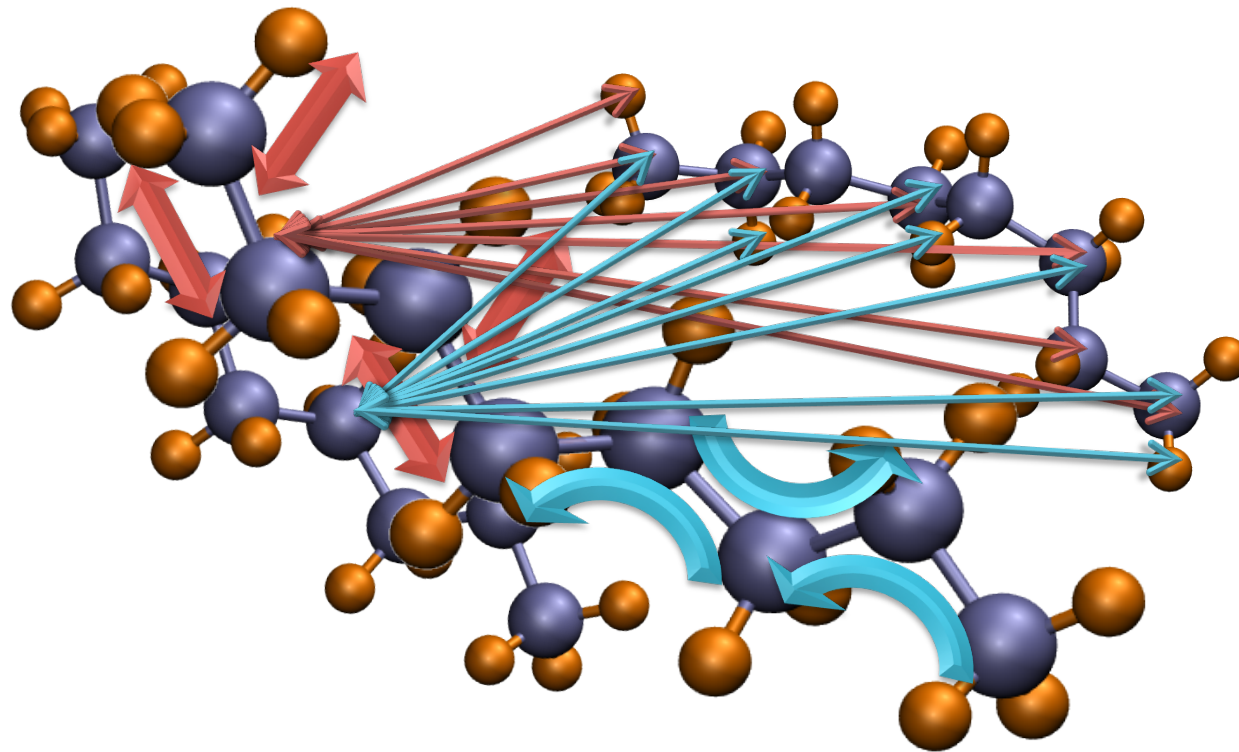


... but



How to include molecular structures?

MD & all-atom potentials



Green-Kubo formula

$$D_{12} = Q \left[x_2 D_1 + x_1 D_2 + x_1 x_2 \left(\frac{f_{11}}{x_1^2} + \frac{f_{22}}{x_2^2} - 2 \frac{f_{12}}{x_1 x_2} \right) \right]$$

Diagram illustrating the components of the Green-Kubo formula for the diffusion coefficient D_{12} :

- Thermodynamic factor** (Q)
- Auto correlation** (D_1 , D_2)
- Cross correlation** (f_{11} , f_{22} , f_{12})
- Mole fraction** (x_1 , x_2)

D as ensemble average of velocity functions

$$D_\alpha = \frac{1}{3} \int_0^\infty \left\langle \vec{u}_i^\alpha(t) \cdot \vec{u}_i^\alpha(t + \Delta t) \right\rangle dt \quad f_{\alpha\beta} = \frac{1}{3} \int_0^\infty \left\langle \vec{u}^\alpha(t) \cdot \vec{u}^\beta(t + \Delta t) \right\rangle dt$$

Computational details

Canonical ensemble (NVT)

- Global thermostat

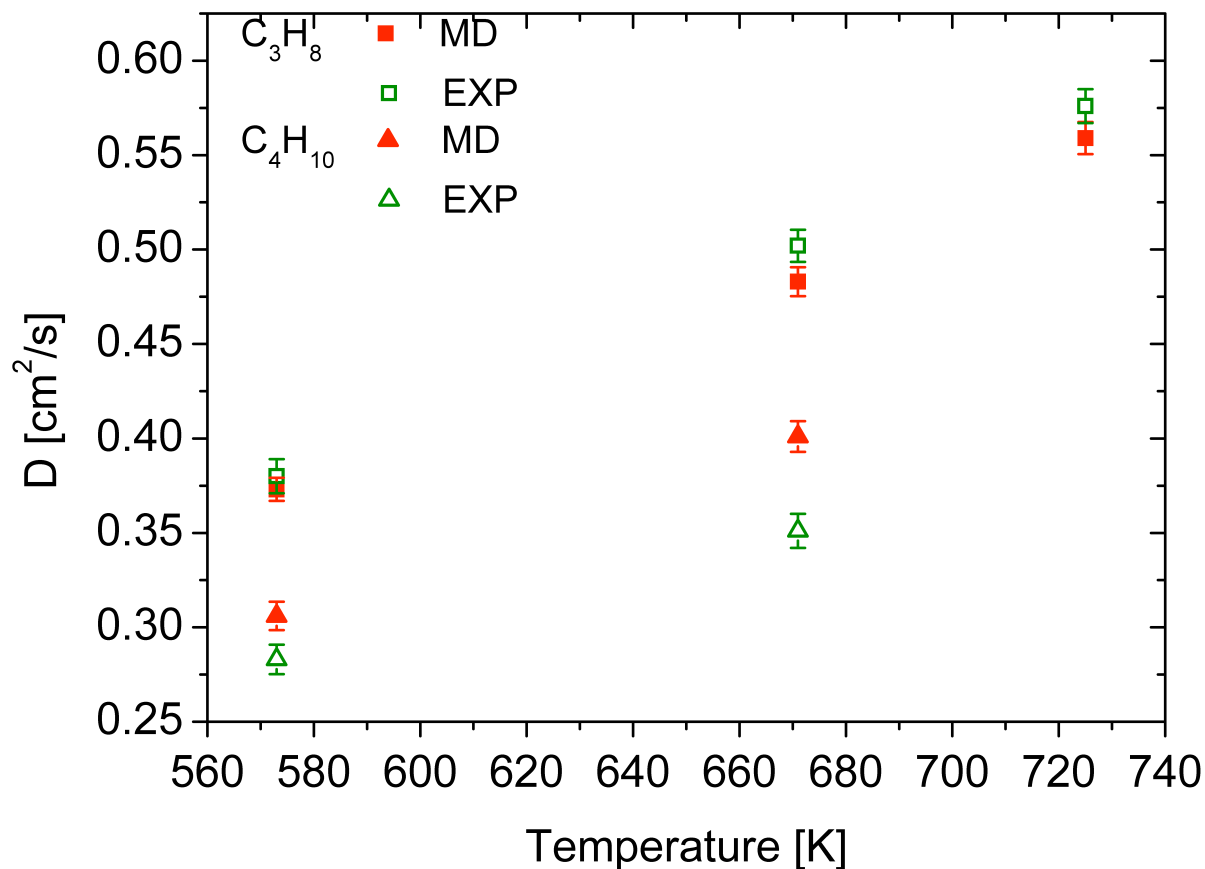
300 alkanes + 3000 nitrogens

- 500 ~ 1000K, 1 atm

Molecules as fully flexible - bond stretching, angle vibration, and change of torsion angle.

Benchmark

Comparison with available experimental data^[1,2]



Good agreement with EXP.

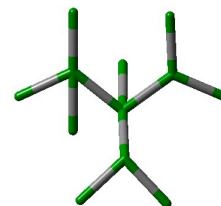
[1] A. Manion et. al., *Combustion inst. tech. meeting*, 2008

[2] W. A. Wakeham et. al., *J. Phys B*, 1973, Vol 6, pp. 886

N-dodecane



$D_{12} [cm^2/s]$

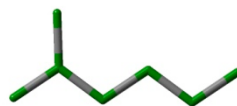


T(K)	MD – d ₁	C-E	MD – d ₂
500	0.1105	0.1351	0.1267
1000	0.3913	0.4705	0.4355
1500	0.8021	0.9446	0.9027

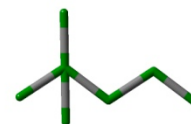
Heptane isomers



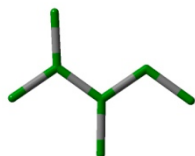
$n\text{-C}_7\text{H}_{16}$
normal heptane



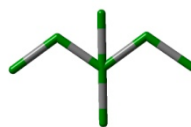
$2\text{-C}_7\text{H}_{16}$
2-methylhexane



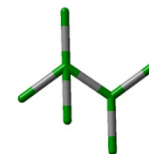
$2,2\text{-C}_7\text{H}_{16}$
2,2-dimethylpentane



$2,3\text{-C}_7\text{H}_{16}$
2,3-dimethylpentane



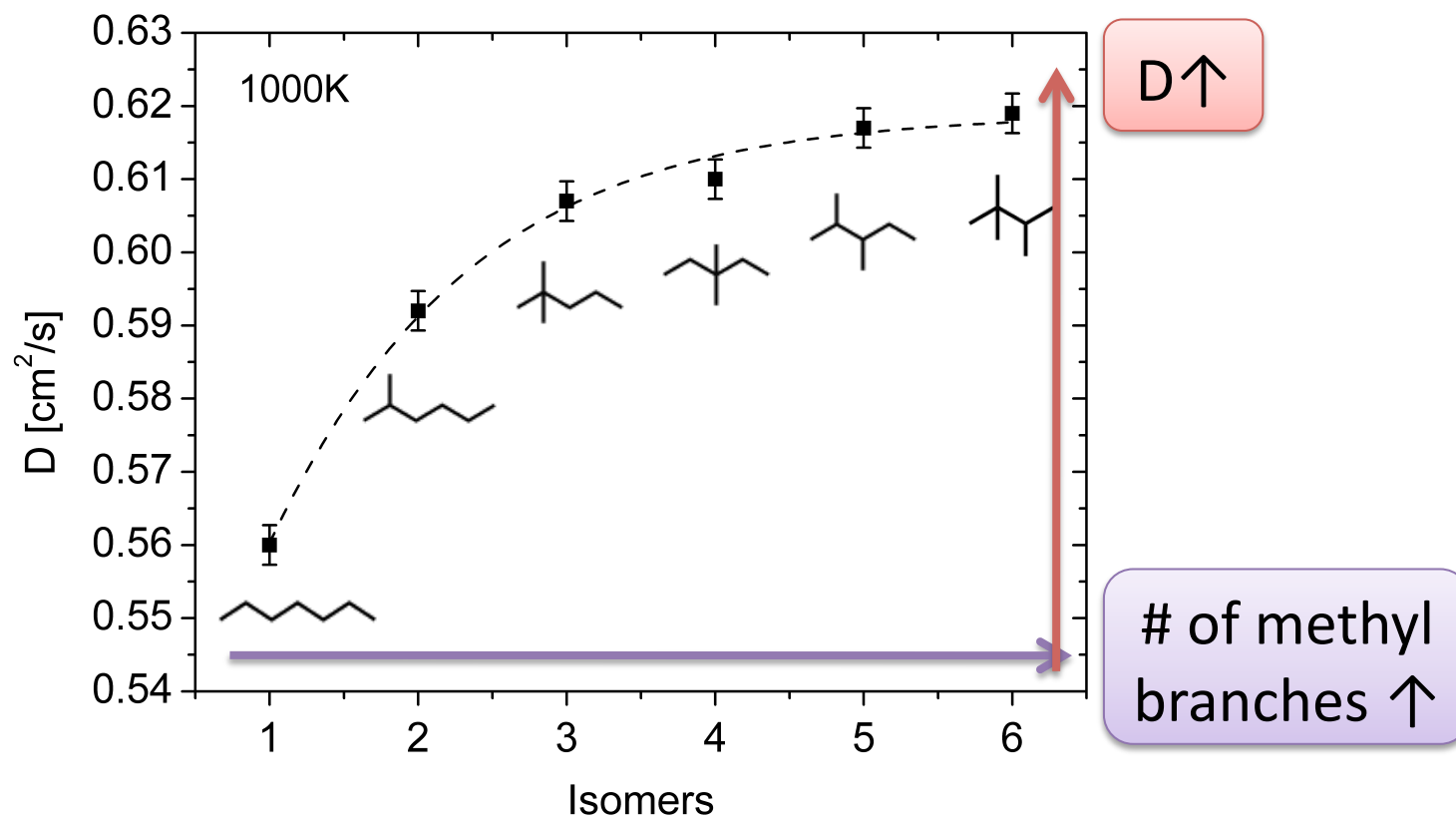
$3,3\text{-C}_7\text{H}_{16}$
3,3-dimethylpentane



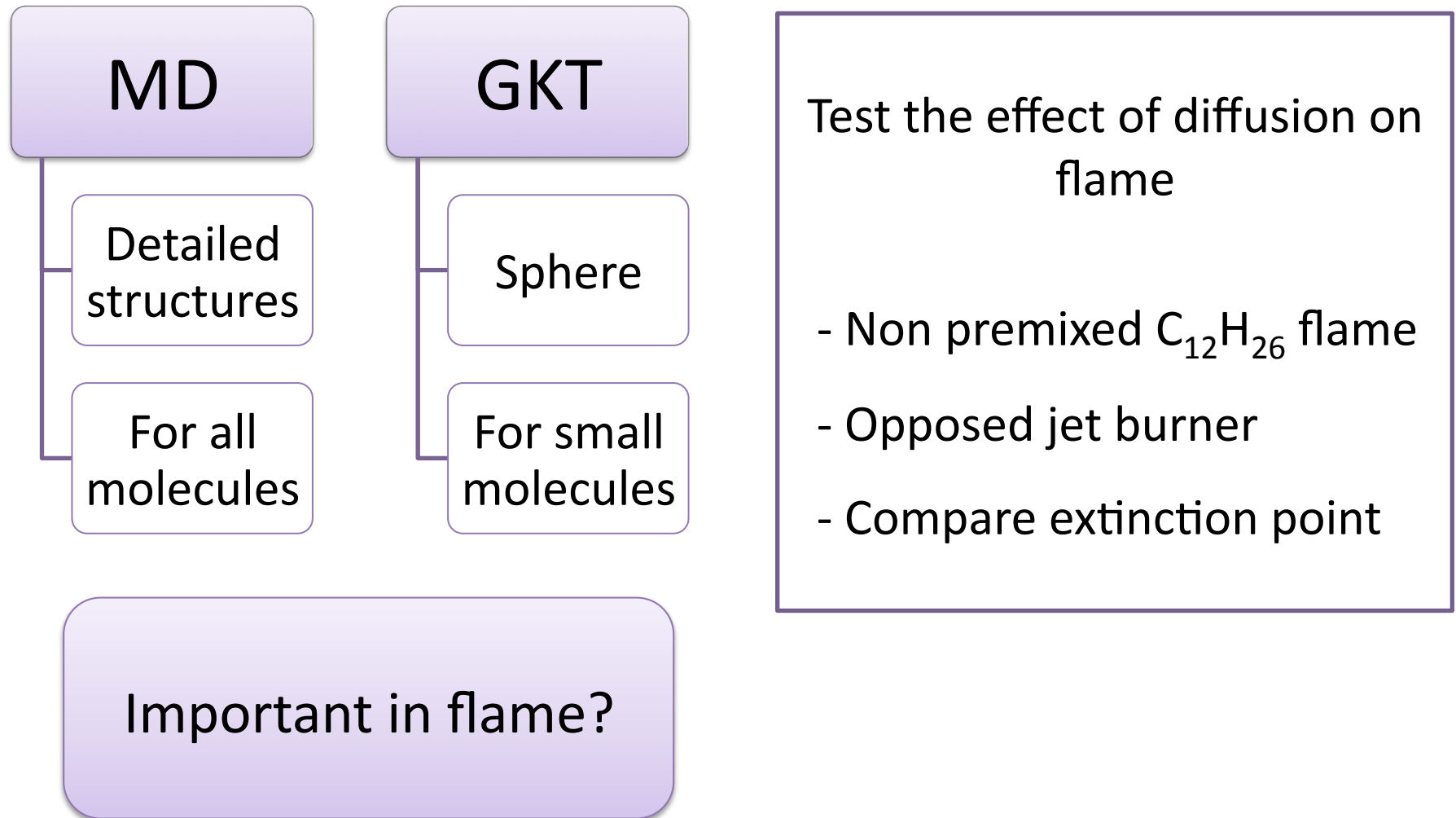
$2,2,3\text{-C}_7\text{H}_{16}$
2,2,3-trimethylbutane

Chae, Violi, J. Chemical Physics, in press

Diffusion coefficients

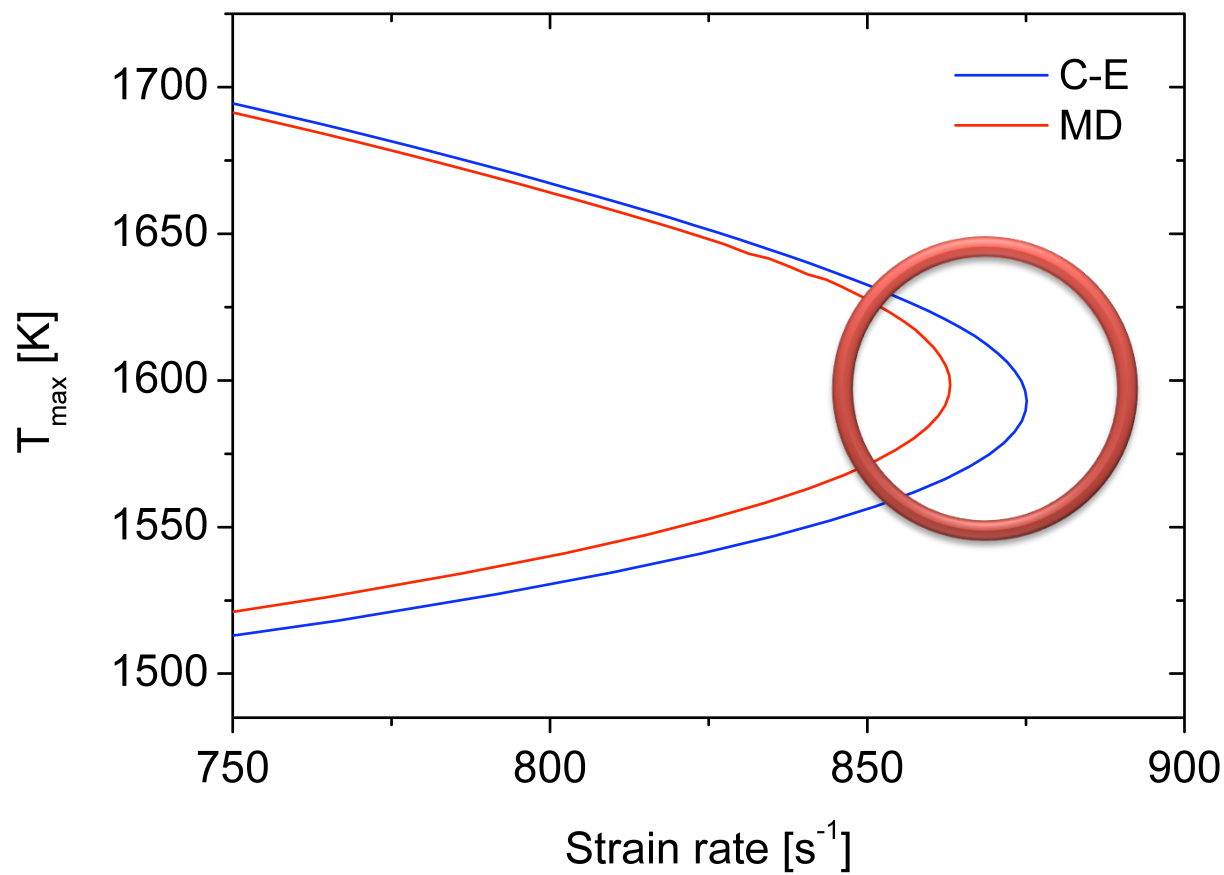


Effect on flame



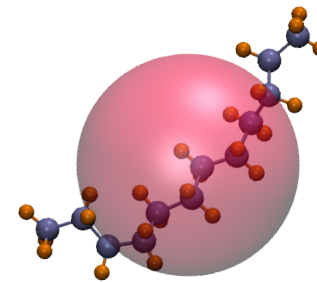
Extinction

$C_{12}H_{26}$ non-premixed opposed jet flame

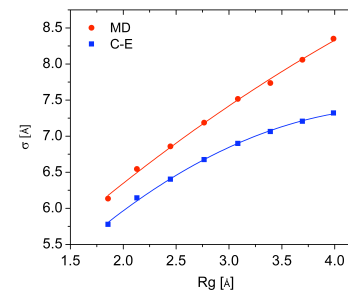


Conclusions

- ❑ Gas kinetic theory (GKT) becomes inaccurate as non-sphericity of a molecule increases.



- ❑ The root of the error in GKT is the assumption of spherical structures for particles.



- ❑ MD can quantify the effect of molecular structures and provide correction factors for GKT (R_g) .